

# BASIC STRUCTURAL ANALYSIS

## CIVIL ENGINEERING VIRTUAL LABORATORY

EXPERIMENT: 3

CONTINUOUS BEAMS

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### INTRODUCTION:

Continuous beams, which are beams with more than two supports and covering more than one span, are not statically determinate using the static equilibrium laws

$e$  = strain

$\sigma$  = stress ( $\text{N/m}^2$ )

$E$  = Young's Modulus =  $\sigma / e$  ( $\text{N/m}^2$ )

$y$  = distance of surface from neutral surface (m).

$R$  = Radius of neutral axis (m).

$I$  = Moment of Inertia ( $\text{m}^4$  - more normally  $\text{cm}^4$ )

$Z$  = section modulus =  $I/y_{\max}$  ( $\text{m}^3$  - more normally  $\text{cm}^3$ )

$M$  = Moment (Nm)

$w$  = Distributed load on beam (kg/m) or (N/m as force units)

$W$  = total load on beam (kg ) or (N as force units)

$F$  = Concentrated force on beam (N)

$L$  = length of beam (m)

$x$  = distance along beam (m)

### OBJECTIVE:

To find the shear force diagram and bending moment diagram for a given continuous beam.

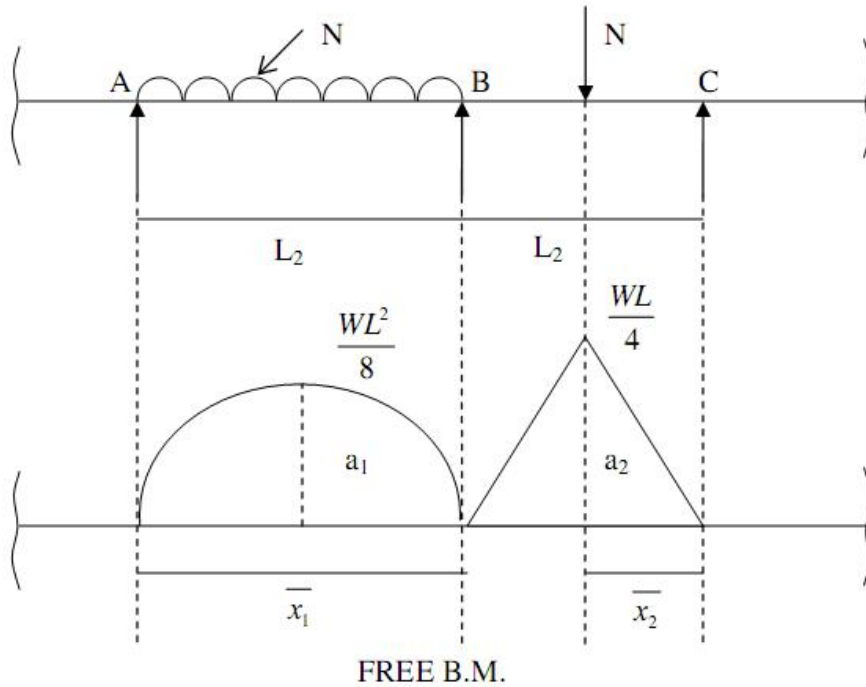
### THEORY:

Beams placed on more than 2 supports are called continuous beams. Continuous beams are used when the span of the beam is very large, deflection under each rigid support will be equal zero.

BMD for Continuous beams:

BMD for continuous beams can be obtained by superimposing the fixed end moments diagram over the free bending moment diagram.

Three - moment Equation for continuous beams THREE MOMENT EQUATION



$$M_A \left( \frac{L_1}{E_1 I_1} \right) + 2M_B \left( \frac{L_1}{E_1 I_1} + \frac{L_2}{E_2 I_2} \right) + M_C \left( \frac{L_2}{E_2 I_2} \right) = \frac{-6a_1 \bar{x}_1}{E_1 I_1 L_1} - \frac{6a_2 \bar{x}_2}{E_2 I_2 L_2} - 6 \left[ \frac{\delta_A - \delta_B}{L_1} + \frac{\delta_C - \delta_B}{L_2} \right]$$

The above equation is called generalized 3-moments Equation.

$M_A$ ,  $M_B$  and  $M_C$  are support moments  $E_1$ ,  $E_2 \rightarrow$  Young's modulus of Elasticity of 2 Spans.

$I_1$ ,  $I_2 \rightarrow$  M O I of 2 spans,

$a_1$ ,  $a_2 \rightarrow$  Areas of free B.M.D.

$\bar{x}_1$  and  $\bar{x}_2 \rightarrow$  Distance of free B.M.D. from the end supports, or outer supports. (A and C)

$\delta_A$ ,  $\delta_B$  and  $\delta_C \rightarrow$  are sinking or settlements of support from their initial position.

Normally Young's modulus of Elasticity will be same throughout than the Equation reduces to

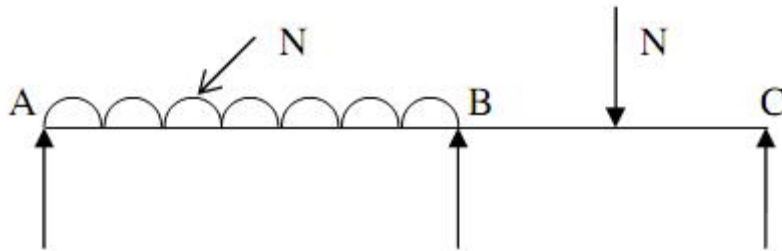
$$M_A \left( \frac{L_1}{I_1} \right) + 2M_B \left( \frac{L_1}{I_1} + \frac{L_2}{I_2} \right) + M_C \left( \frac{L_2}{I_2} \right) = \frac{-6a_1 \bar{x}_1}{I_1 L_1} - \frac{6a_2 \bar{x}_2}{I_2 L_2} - 6 \left[ \frac{\delta_A - \delta_B}{L_1} + \frac{\delta_C - \delta_B}{L_2} \right]$$

If the supports are rigid then  $\delta_A = \delta_B = \delta_C = 0$

$$M_A L_1 + 2M_B (L_1 + L_2) + M_C L_2 = \frac{-6a_1 \bar{x}_1}{L_1} - \frac{6a_2 \bar{x}_2}{L_2}$$

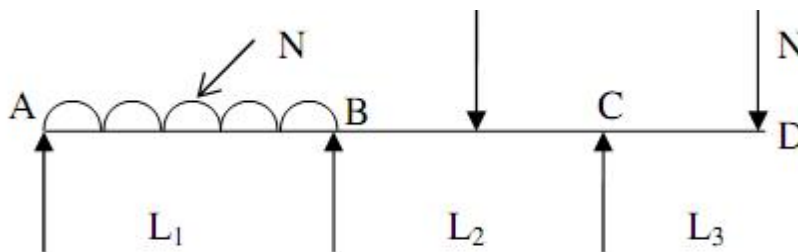
Note:

1.



If the end supports are simple supports then  $M_A = M_C = 0$ .

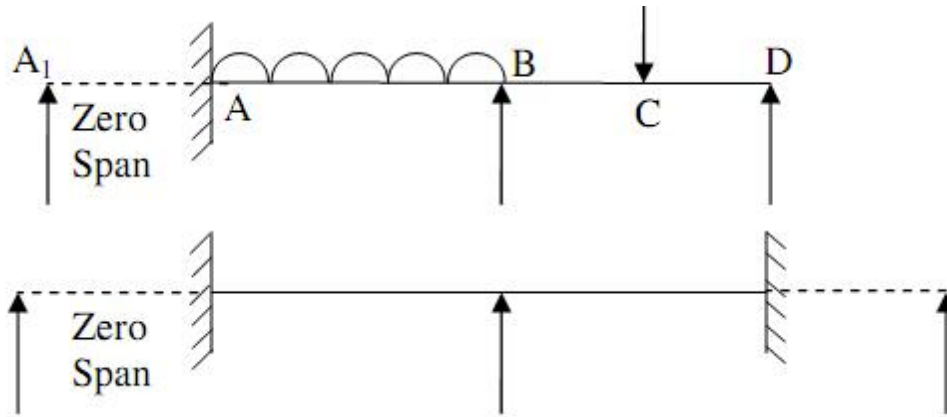
2.



$$M_C = -WL_3$$

If there is an overhang portion then support moment near the overhang can be computed directly.

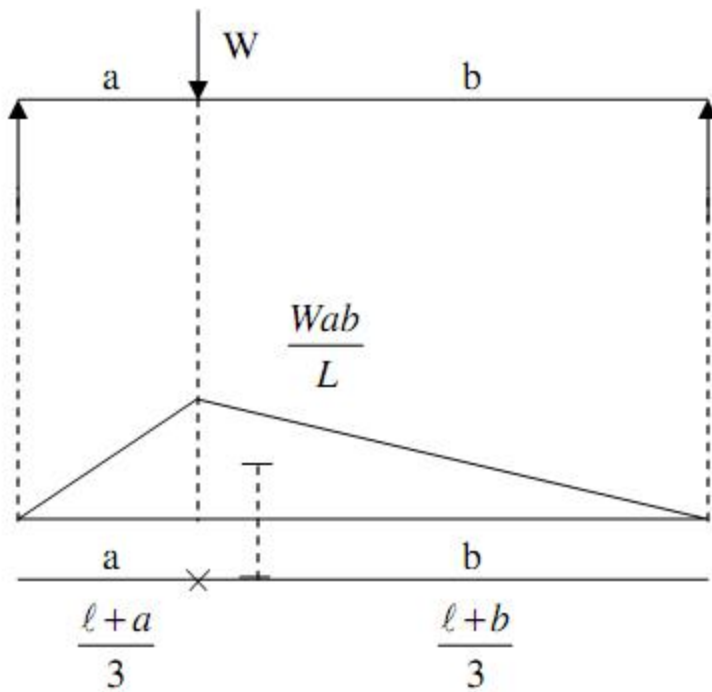
3.



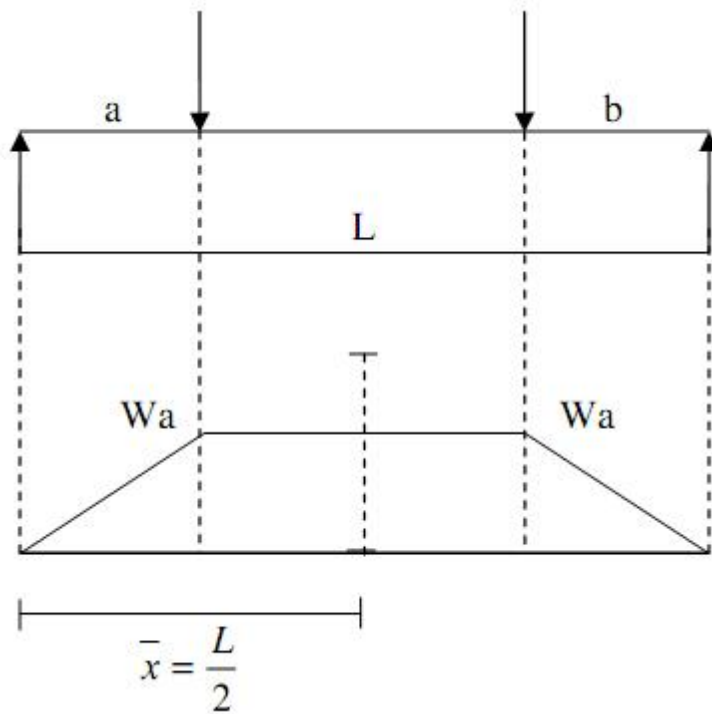
If the end supports are fixed assume an extended span of zero length and apply 3- Moment equation.

NOTE:

i)



In this case centroid lies as shown in the figure.



Observation Table:

Section type	Types of loads	Length of member (L)	Breadth h(b)	Depth(d)	Weight (W)	At a distance from section 'X'	Bending Moment (Knm)	S.F (Kn)	Deflection(Delta)
continuous beams	Two Equal Spans – Uniform Load on One Span								
	Two Equal Spans – Concentrated Load at Center of One Span								

Two Equal Spans – Concentrated Load at Any Point									
Two Equal Spans – Uniformly Distributed Load									
Two Equal Spans – Two Equal Concentrated Loads Symmetrically Placed									
Two Unequal Spans – Uniformly Distributed Load									
Two Unequal Spans – Concentrated Load on Each Span Symmetrically Placed									

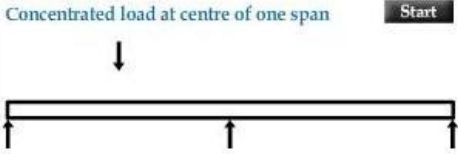
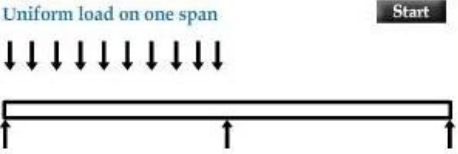
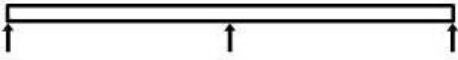
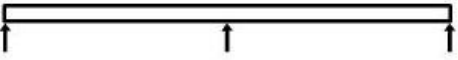
Output:

1. Bending moment\_\_\_\_\_ (Knm)
2. Shear Force\_\_\_\_\_ (KN)
- 3 Deflections\_\_\_\_\_ (Yc)

References:

1. Theory of Structures volume: 1 by S.P.Guptha and G.S.Pandit
2. Reference taken from N.D.S.

PART – 2  
ANIMATION STEPS

Continuous Beams	Two Equal Spans	
		Concentrated load at centre of one span <input type="button" value="Start"/>
◦ Two Equal Spans Concentrated load at centre of one span U D L		
◦ Two Equal Spans Concentrated loads U D L	Deflection of beam	Deflection of beam
◦ Two Unequal Spans Concentrated load on each span U D L		
	SFD	SFD
	BMD	BMD



**PART – 3**  
**VIRTUAL LAB FRAME**